



|     |   |    |
|-----|---|----|
| (b) | $\frac{dx}{dt} = 4 - 2 \sin 2t,$  | B1 |
|     | $\frac{dy}{dt} = 3 \cos 3t$   | B1 |
|     | Use of $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$               | M1 |
|     | Substituting $\frac{\pi}{12}$ for $t$ in expression for $\frac{dy}{dx}$ | m1 |
|     | $\frac{dy}{dx} = \frac{1}{\sqrt{2}}$                                    | A1 |

|    |   |    |
|----|---|----|
| 4. | $f(x) = 4x^3 - 2x - 5$  |    |
|    | An attempt to check values or signs of $f(x)$ at $x = 1, x = 2$                   | M1 |
|    | $f(1) = -3 < 0, f(2) = 23 > 0$  |    |
|    | Change of sign $\Rightarrow f(x) = 0$ has root in (1, 2)                          | A1 |
|    | $x_0 = 1.2$   |    |
|    | $x_1 = 1.227601026$ ( $x_1$ correct, at least 5 places after the point)           | B1 |
|    | $x_2 = 1.230645994$   |    |
|    | $x_3 = 1.230980996$   |    |
|    | $x_4 = 1.231017841 = 1.23102$ ( $x_4$ correct to 5 decimal places)                | B1 |
|    | An attempt to check values or signs of $f(x)$ at $x = 1.231015, x = 1.231025$     | M1 |
|    | $f(1.231015) = -1.197 \times 10^{-4} < 0, f(1.231025) = 4.218 \times 10^{-5} > 0$ | A1 |
|    | Change of sign $\Rightarrow \alpha = 1.23102$ correct to five decimal places      | A1 |

**Note: ‘Change of sign’ must appear at least once.**

|    |     |       |   |    |
|----|-----|-------|---|----|
| 5. | (a) | (i)   | $\frac{dy}{dx} = 13 \times (7 + 2x)^{12} \times f(x), (f(x) \neq 1)$  | M1 |
|    |     |       | $\frac{dy}{dx} = 26 \times (7 + 2x)^{12}$   | A1 |
|    |     | (ii)  | $\frac{dy}{dx} = \frac{5}{\sqrt{1 - (5x)^2}}$ or $\frac{1}{\sqrt{1 - (5x)^2}}$ or $\frac{5}{\sqrt{1 - 5x^2}}$ | M1 |
|    |     |       | $\frac{dy}{dx} = \frac{5}{\sqrt{1 - 25x^2}}$  | A1 |
|    |     | (iii) | $\frac{dy}{dx} = x^3 \times f(x) + e^{4x} \times g(x)$  | M1 |
|    |     |       | $\frac{dy}{dx} = x^3 \times f(x) + e^{4x} \times g(x)$ (either $f(x) = 4e^{4x}$ or $g(x) = 3x^2$ )            | A1 |
|    |     |       | $\frac{dy}{dx} = x^3 \times 4e^{4x} + e^{4x} \times 3x^2$ (all correct)                                       | A1 |

$$(b) \quad \frac{d}{dx} (\tan x) = \frac{\cos x \times m \cos x - \sin x \times k \sin x}{\cos^2 x} \quad (m = \pm 1, k = \pm 1) \quad \text{M1}$$

$$\frac{d}{dx} (\tan x) = \frac{\cos x \times \cos x - \sin x \times (-\sin x)}{\cos^2 x} \quad \text{A1}$$

$$\frac{d}{dx} (\tan x) = \frac{\cos^2 x + \sin^2 x}{\cos^2 x}$$

$$\frac{d}{dx} (\tan x) = \frac{1}{\cos^2 x} = \sec^2 x \quad (\text{convincing}) \quad \text{A1}$$

6. (a) (i)  $\int (7x-9)^{1/2} dx = k \times \frac{(7x-9)^{3/2}}{3/2} + c \quad (k = 1, 7, 1/7) \quad \text{M1}$

$$\int (7x-9)^{1/2} dx = 1/7 \times \frac{(7x-9)^{3/2}}{3/2} + c \quad \text{A1}$$

(ii)  $\int e^{x/6} dx = k \times e^{x/6} + c \quad (k = 1, 6, 1/6) \quad \text{M1}$

$$\int e^{x/6} dx = 6 \times e^{x/6} + c \quad \text{A1}$$

(iii)  $\int \frac{4}{5x-1} dx = 4 \times k \times \ln |5x-1| + c \quad (k = 1, 5, 1/5) \quad \text{M1}$

$$\int \frac{4}{5x-1} dx = 4 \times 1/5 \times \ln |5x-1| + c \quad \text{A1}$$

(b)  $\int (3x-4)^{-3} dx = k \times \frac{(3x-4)^{-2}}{-2} \quad (k = 1, 3, 1/3) \quad \text{M1}$

$$\int_2^4 8 \times (3x-4)^{-3} dx = \left[ 8 \times \frac{1}{3} \times \frac{(3x-4)^{-2}}{-2} \right]_2^4 \quad \text{A1}$$

Correct method for substitution of limits M1

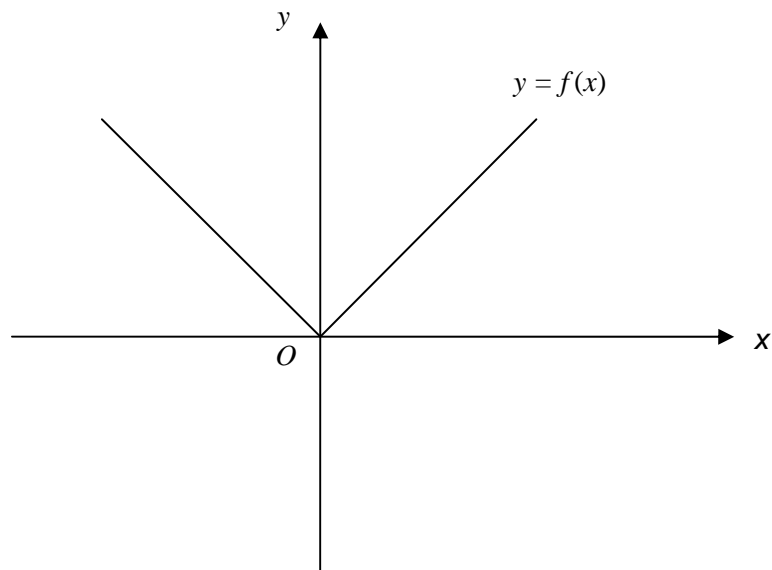
$$\int_2^4 8 \times (3x-4)^{-3} dx = \frac{5}{16} = 0.3125 \quad (\text{f.t. for } k = 1, 3 \text{ only}) \quad \text{A1}$$

7. (a) Trying to solve either  $3x + 1 \leq 5$  or  $3x + 1 \geq -5$  M1  
 $3x + 1 \leq 5 \Rightarrow x \leq \frac{4}{3}$   
 $3x + 1 \geq -5 \Rightarrow x \geq -2$  (both inequalities) A1  
 Required range:  $-2 \leq x \leq \frac{4}{3}$  (f.t. one slip) A1

**Alternative mark scheme**

- $(3x + 1)^2 \leq 25$  (forming and trying to solve quadratic) M1  
 Critical points  $x = -2$  and  $x = \frac{4}{3}$  A1  
 Required range:  $-2 \leq x \leq \frac{4}{3}$  (f.t. one slip in critical points) A1

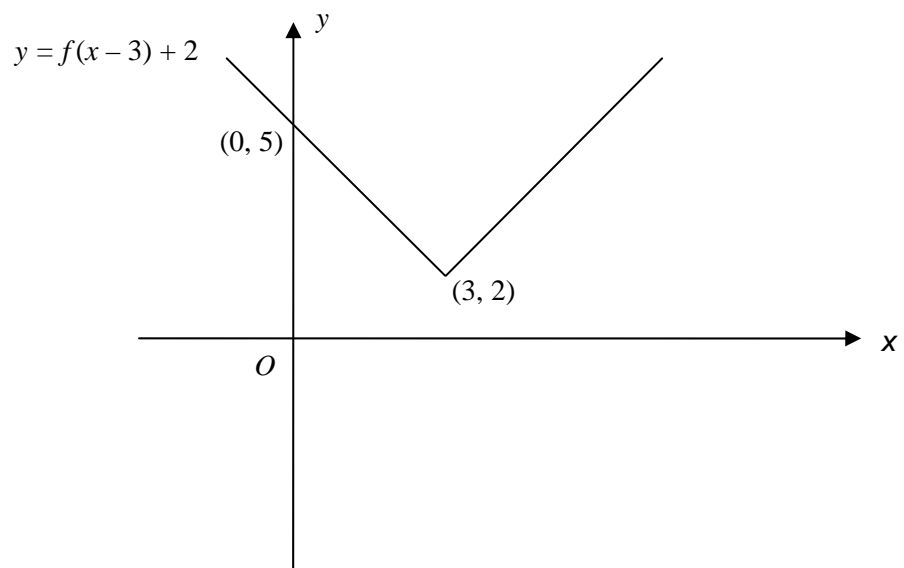
- (b) (i)



Correct graph

B1

- (ii)



- Translation of graph of  $f(x) = |x|$  with vertex at  $(\pm 3, \pm 2)$  M1  
 Coordinates of vertex =  $(3, 2)$  A1  
 Crosses y-axis at  $(0, 5)$  A1

8. (a)  $g'(x) = \frac{3 \times f(x)}{4x^2 + 9} + 2 \quad f(x) \neq 1$  M1  
 $g'(x) = \frac{3 \times 8x}{4x^2 + 9} + 2$  A1  
 $g'(x) = \frac{24x + 8x^2 + 18}{4x^2 + 9} = \frac{2(2x + 3)^2}{4x^2 + 9}$  (convincing) A1
- (b) (i) At stationary point,  $\frac{2(2x + 3)^2}{4x^2 + 9} = 0$   
or  $\frac{3 \times 8x}{4x^2 + 9} + 2 = 0$  M1  
 $\frac{2(2x + 3)^2}{4x^2 + 9} = 0$  only when  $x = -\frac{3}{2}$  A1
- (ii)  $g'(x) > 0$  either side of  $x = -\frac{3}{2}$  (or at all other points) M1  
Stationary point is a point of inflection A1
9. (a)  $y - 5 = \ln(3x - 2)$  B1  
An attempt to express candidate's equation as an exponential equation M1  
 $x = \frac{(e^{y-5} + 2)}{3}$  (f.t. one slip) A1  
 $f^{-1}(x) = \frac{(e^{x-5} + 2)}{3}$  (f.t. one slip) A1
- (b)  $D(f^{-1}) = [5, \infty)$  B1
10. (a)  $R(f) = [1, \infty)$  B1  
 $R(g) = [-3, \infty)$  B1
- (b)  $gf(x) = 2\sqrt{(x + 4)^2} - 3.$  M1  
 $gf(x) = 2x + 5$  A1
- (c)  $fg(x) = \sqrt{2x^2 - 3 + 4}$  (correct composition) B1  
 $[fg(x)]^2 = 17^2$  (candidate's  $fg(x)$ ) M1  
 $x^2 = 144$  (f.t. one numerical slip) A1  
 $x = \pm 12$  (c.a.o.) A1