

PARAMETRIC EQUATIONS

A2 Unit 3: Pure Mathematics B

WJEC past paper questions: 2010 – 2017

Total marks available 74 (approximately 1 hour 30 minutes)

1.

The parametric equations of the curve C are

$$x = \frac{2}{t}, y = 4t.$$

(a) Show that the tangent to C at the point P with parameter p has equation

$$y = -2p^2x + 8p. \quad [4]$$

(b) The tangent to C at the point P passes through the point $(2, 3)$. Show that P can be one of two points. Find the coordinates of each of these two points. [4]

(Summer 10)

2.

The curve C has the parametric equations

$$x = 3 \cos t, y = 4 \sin t.$$

The point P lies on C and has parameter p .

(a) Show that the equation of the tangent to C at the point P is

$$(3 \sin p)y + (4 \cos p)x - 12 = 0. \quad [5]$$

(b) The tangent to C at the point P meets the x -axis at the point A and the y -axis at the point B . Given that $p = \frac{\pi}{6}$,

(i) find the coordinates of A and B ,

(ii) show that the exact length of AB is $2\sqrt{19}$. [4]

(Summer 11)

3. The parametric equations of the curve C are $x = t^2, y = 2t$.

(a) Show that the normal to C at the point P with parameter p has equation

$$y + px = p^3 + 2p. \quad [5]$$

(b) The normal to C at the point P intersects C again at the point with parameter 3.

(i) Show that $p^3 - 7p - 6 = 0$.

(ii) Hence show that P can be one of two points. Find the coordinates of each of these two points. [6]

(Summer 12)

4. The curve C has the parametric equations

$$x = at, y = \frac{b}{t},$$

where a, b are positive constants.

The point P lies on C and has parameter p .

(a) Show that the equation of the tangent to C at the point P is

$$ap^2y + bx - 2abp = 0. \quad [5]$$

(b) The tangent to C at the point P meets the x -axis at the point A and the y -axis at the point B . Find the area of triangle AOB , where O denotes the origin. Give your answer in its simplest form. [3]

(c) The point D has coordinates $(2a, b)$. Show that there is no point P on C such that the tangent to C at the point P passes through D . [3]

(Summer 13)

5. The curve C has the parametric equations $x = 2t, y = 5t^3$. The point P lies on C and has parameter p .

(a) Show that the equation of the tangent to C at the point P is

$$2y = 15p^2x - 20p^3. \quad [4]$$

(b) The tangent to C at the point P intersects C again at the point $Q(2q, 5q^3)$. Given that $p = 1$, show that q satisfies the equation

$$q^3 - 3q + 2 = 0.$$

Hence find the value of q . [5]

(Summer 14)

6. The parametric equations of the curve C are $x = at^2$, $y = 2at$, where a is a positive constant. The points P and Q lie on C and have parameters p and q respectively.

- (a) Simplifying your answer in each case, find
- (i) the gradient of the tangent to C at the point P ,
 - (ii) the equation of the tangent to C at the point P . [4]
- (b) (i) Find an expression, in its simplest form, for the gradient of the line PQ .
- (ii) Explain how you could use the answer of (b)(i) to derive the gradient of the tangent to C at the point P . [4]

(Summer 15)

7. The parametric equations of the curve C are

$$x = \frac{3}{t}, \quad y = 4t.$$

- (a) Show that the tangent to C at the point P with parameter p has equation
- $$3y = -4p^2x + 24p. \quad [4]$$
- (b) The tangent to C at the point P passes through the point $(1, 9)$. Show that P can be one of two points. Find the coordinates of each of these two points. [4]

(Summer 16)

8. The curve C has the parametric equations $x = at^2$, $y = bt^3$, where a, b are positive constants. The point P lies on C and has parameter p .

- (a) Show that the equation of the tangent to C at the point P is
- $$2ay = 3bpx - abp^3. \quad [5]$$

- (b) The tangent to C at the point P intersects C again at the point with coordinates $(4a, 8b)$. Show that p satisfies the equation

$$p^3 - 12p + 16 = 0.$$

Hence find the value of p . [5]

(Summer 17)